A novel physics-inspired method for image region segmentation by imitating the carrier immigration in semiconductor materials

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Abstract. A novel method for image region segmentation is proposed, which is inspired by the carrier immigration mechanism in semiconductor materials. The carrier diffusing and drifting are simulated in the proposed model, and the sign distribution of net carrier at the model’s balance state is exploited for region segmentation. The experiments have been done for test images and real world images, which prove the effectiveness of the proposed method.

1 Introduction

Self balancing is a mechanism existing in many natural systems. For example, the formation of the P-N junction in semiconductor materials is the result of balancing of the diffusing and drifting process of carriers. The physical P-N junction, the charge carriers in P-type and N-type semiconductor are holes and electrons respectively [1,2]. When the materials of the two are put together with compact contact, diffusion of carries will happen at the interface of contact due to carrier density difference (i.e. carrier moving from high-density side to low density side). Meanwhile, a space charge region is established. It in turn causes the drifting of carriers which is at the opposite direction of diffusing. The above process will reach a balance state [1,2]. In the self balancing mechanism shown in Figure. 1, the system’s state at new balancing point may depend on the external influence (such as the external voltage applied onto the P-N junction). This mechanism may be the inspiration of novel methods for problem solving, if the self balancing mechanism suits the nature of the problem well.

2 The model of virtual carrier immigration in digital images

The proposed model for image segmentation is as follows. Two categories of virtual carriers are defined: positive and negative, which imitates the physical electron and hole. Each pixel is modelled as a container of virtual carriers. Each pixel has four adjacent pixels (except those on image borders), and correspondingly each carrier container has four adjacent containers. There is an interface between each pair of adjacent containers. There are two features of the interface mentioned above. Firstly, the interface has permeability, which means the carriers at both sides of the surface can diffuse through it due to density difference. Secondly, there is a virtual electric field imposed on it, whose direction and intensity are determined by the greyscale difference between the corresponding two pixels connected by that interface. The virtual electric field is defined as:

\[ \mathbf{E} = \frac{\nabla I}{\rho} \]

where \( \mathbf{E} \) is the electric field, \( \nabla I \) is the greyscale difference between two pixels, and \( \rho \) is the density of carriers.

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\[ e = K \cdot (g - g_a) \]  

where \( e \) is the intensity of virtual electric field at the interface, \( K \) is a predefined positive coefficient, \( g \) is the greyscale of the pixel of interest and \( g_a \) is that of its adjacent pixel. The effect of each virtual electric field is limited to its corresponding interface only, and does not influence other interfaces. In such a way, the model is established consisting of virtual carrier containers and their interfaces, the virtual electric field, and also the virtual carriers.

The evolution of the system is analyzed as follows. Initially, suppose the positive and negative carriers are of the same quantity, and each container has the same amount of carriers. Also suppose all the containers have the same volume, so that the density of carrier in a container is proportional to the amount of carrier in it. Therefore, there is no density difference of carriers between adjacent containers at that time. In another word, there is no carrier diffusion at the beginning. However, due to the virtual electric field at each interface, the positive and negative carriers drift across the interfaces due to the virtual force applied by the electric field. The drifting then causes carrier density difference between two sides of the interface, which in turn makes the carriers to diffuse due to that density difference. Obviously, the diffusion has the opposite effect of drifting. For each interface and each container, such dynamic process evolves until a balance between drifting and diffusion is reached. Figure 2 shows the details of carrier immigration between two adjacent containers, while Figure 3 shows the overall structure of the model on digital image. The balance state is worth of study for possible use in image segmentation, and difference of the proposed algorithm and the physical process can also be clearly seen as above.

![Figure 2](image1.png)

**Fig. 2.** Two adjacent containers in the proposed model of carrier immigration in digital images.

![Figure 3](image2.png)

**Fig. 3.** The structure of the proposed model upon digital image.

### 3 Image segmentation based on virtual carrier immigration

#### 3.1 Model implementation by computer simulation

In the simulation of the model on computer, the simulation must be implemented in discrete steps (i.e. iteration by iteration). In one simulation step, the drifting speed of carrier (i.e. the amount of carrier immigrating from one container to the other in an iteration of simulation, or one simulation step) is defined directly proportional to the intensity of virtual electric field:

\[ \Delta c_{drifting} = K_1 \cdot e \]  

where \( \Delta c_{drifting} \) is the amount of carrier drifting from one container into the other, \( K_1 \) is a predefined positive coefficient, \( e \) is the intensity of virtual electric field at the interface. According to Equation (1), \( \Delta c_{drifting} \) is also proportional to the greyscale difference between the adjacent pixels:

\[ \Delta c_{drifting} = K_1 \cdot (g - g_a) \]  

where \( \Delta c_{drifting} \) is the amount of carrier drifting from one container into the other, \( K_1 \) is a predefined positive coefficient, \( g \) is the greyscale of the pixel of interest and \( g_a \) is that of its adjacent pixel.

On the other hand, in one simulation step, the speed of diffusion has proportionality relationship with carrier density difference between the adjacent pixels. Suppose each container has the same size (or volume). Then the carrier density is proportional to the carrier amount in each container. Therefore, in the implementation the carrier density is substituted by carrier amount for diffusing:

\[ \Delta c_{diffusing} = K_2 \cdot (c - c_a) \]  

where \( \Delta c_{diffusing} \) is the amount of carrier diffusing from one container into the other, \( K_2 \) is a predefined positive coefficient, \( c \) is the net carrier amount in the container of interest and \( c_a \) is that in its adjacent container. There are two types of carriers in the model: positive and negative. Each container has both types in it. In the evolving process, the two types of carrier immigrate by drifting and diffusing respectively. For each container, the net carrier is the combination of the two types after the offset between them. For simplicity in implementation, the immigration of carriers is measured by the amount of net carrier. In another word, the carrier density and the flow of carrier between containers are measured by net carrier amount.

The process of implementing the model is as follows. At the beginning, the amounts of positive and negative carriers are equal in each container. Also suppose the amount is sufficient for arbitrary amount of carrier immigration in the simulation. Then the virtual electric field is calculated at each interface between adjacent containers, which is proportional to the greyscale difference between corresponding adjacent pixels. The detailed simulation step is as follows:

**Step 1** For each of the four interfaces of every virtual container (or pixel), do the following: calculate the
drifting amount of carrier due to virtual electric field; calculate the diffusing amount of carrier due to carrier density difference; sum the above two for all the 4 interfaces of a container to get its total change of net carrier amount; update the net carrier amount in that container;

**Step2.** After all the containers update their net carrier amount, calculate the average change of net carrier for all the containers. If the average change of net carrier is smaller than a predefined threshold, it is close enough to the balance state, and the simulation stops; otherwise, return to **Step1** to begin a new iteration of simulation.

### 3.3 Image segmentation based on the proposed model for real world images

In the above experimental results for the test images, it is shown that the sign of net carrier are opposite in two adjacent regions, which can provide the basis of region division in images. In order to obtain the segmentation result from the sign distribution of the net carrier, a region grouping approach is proposed as following:

#### Step1
Implement the simulation of the virtual carrier immigration as proposed in section 4.1;

**Step2:** Obtain the sign distribution of the net carrier;

**Step3:** Group the adjacent containers (i.e. image points) with the same sign of net carrier as connected points in same region. In the region grouping process, the adjacent pixels of the 4-connection (i.e. the upper, lower, left and right pixels) for an image point $p$ is investigated.

However, real world images are more complex. To investigate the effect of the proposed method, experiments are carried out for a series of real world images. For demonstration, an example of the results is shown in Figure. 5, which is for the medical heart image. The experimental results indicate that the proposed method can obtain large amount of regions (more than a hundred). There are 533 for the medical heart image. To obtain practically useful segmentation result, a region merging method is proposed based on the gray-scale similarity of adjacent regions. Given an expected number of remaining regions after merging, the following steps are carried out to merge regions:

**Step1:** Calculate its average gray-scale value for each region.

**Step2:** Find the pair of neighboring regions with the least difference of the average gray-scale, and merge them into one region.

**Step3:** If current region number is larger than the expected number, return to **Step1**; otherwise, stop the merging.
In Figure 5, the following results show the original image, the sign distribution of net carrier at the balance state, the region segmentation results by grouping, and also the result of region merging. In the sign distribution of net carrier, the white points represent positive net carrier, and black points represent negative net carrier. In the region segmentation results and region merging results, different regions are represented by different greyscale values. For the medical image of the heart, the remained region number after merging is 50 in Figure 5(d). Figure 5(d) shows the heart structure clearly. Moreover, the average of the net carrier change for all the points is calculated and recorded as a measurement of the convergence degree to the balance state. Figure 6 shows the relationship between that average value and the simulation time, which indicates that the process of carrier immigration approaches the balance state with the simulation going on. The experimental results prove that the proposed method is effective in segmentation of real world images.

4 Conclusion

A novel model of virtual carrier immigration is presented by imitating the diffusing and drifting of carriers in physical P-N junction. The virtual electric field between adjacent pixels is defined according to their greyscale difference, which is the major difference between the proposed model and real P-N junction. The direct local interaction and indirect global interaction of the above two carrier movements can lead to a balance state of carrier distribution, which provides clues for region segmentation. Image segmentation is implemented based on the sign distribution of net carrier at balance state, and a merging step is applied to get more comprehensible and useful segmentation results. The experimental results for test images and real world images prove the effectiveness of the proposed method. For future improvement of the segmentation results, color and texture feature will also be introduced into segmentation for possible improvement.

Fig. 5. The experimental results for the medical heart image.

Fig. 6. The relationship between the average change of net carrier and the simulation time (for the medical heart image).

References